

# Quasi-Integrable Optics Experiment at IOTA

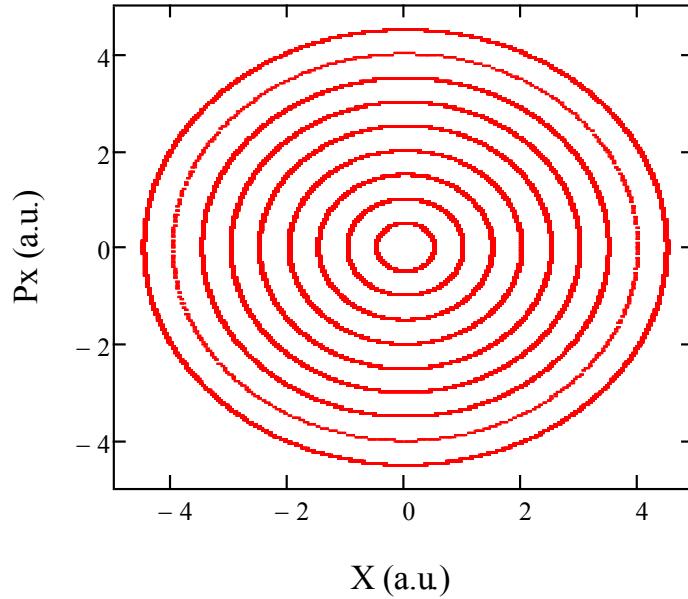
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# Motivation: linear dynamics

- Linear focusing lattice – betatron tunes of different particles are almost equal
- In ideal case, particle motion is unconditionally stable

Phase space trajectories of perfectly linear 1D motion in normalized coordinates

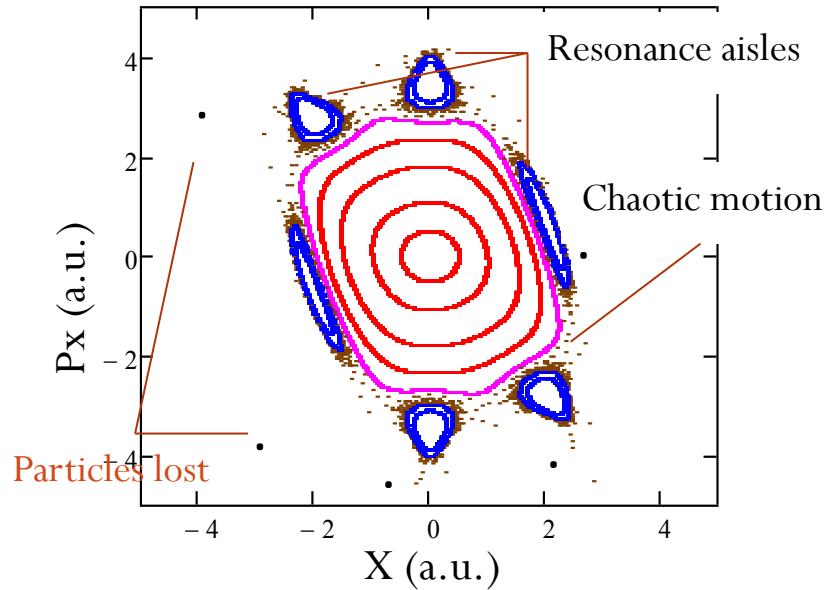


# Motivation: linear dynamics

- Linear focusing lattice – betatron tunes of different particles are almost equal
- Nonlinearities (both magnet imperfections and specially introduced) make single particle motion unstable due to resonances
- Hamiltonian depends on time

- Stability depends on initial conditions

Phase space of 1D motion in linear lattice with 1 octupole nonlinearity

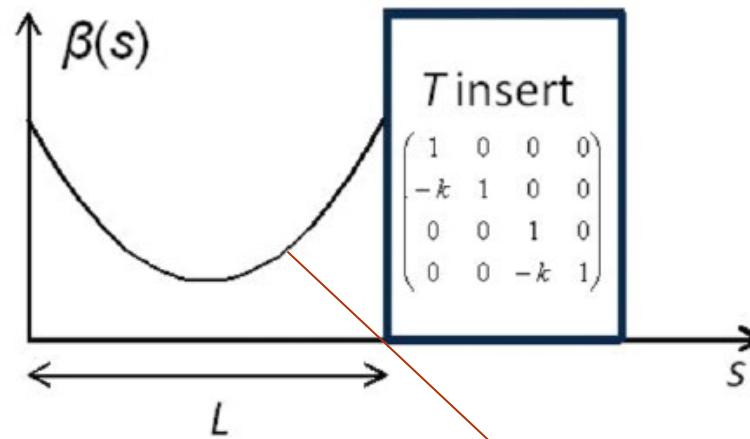


# Motivation: nonlinear dynamics

- Tunes depend on amplitude
- Landau Damping increases with the spread of betatron oscillation frequencies. Larger tune spread → beam more stable against collective instabilities.
  - Can be created by adding octupole magnets
- If the system is integrable – no resonances
- IOTA Goal: create practical nonlinear accelerator focusing systems with a large frequency spread and stable particle motion.

# Nonlinear lattice with two invariants

- Danilov, Nagaitsev, Phys. Rev. ST Accel. Beams 13, 2010
- Element of periodicity:



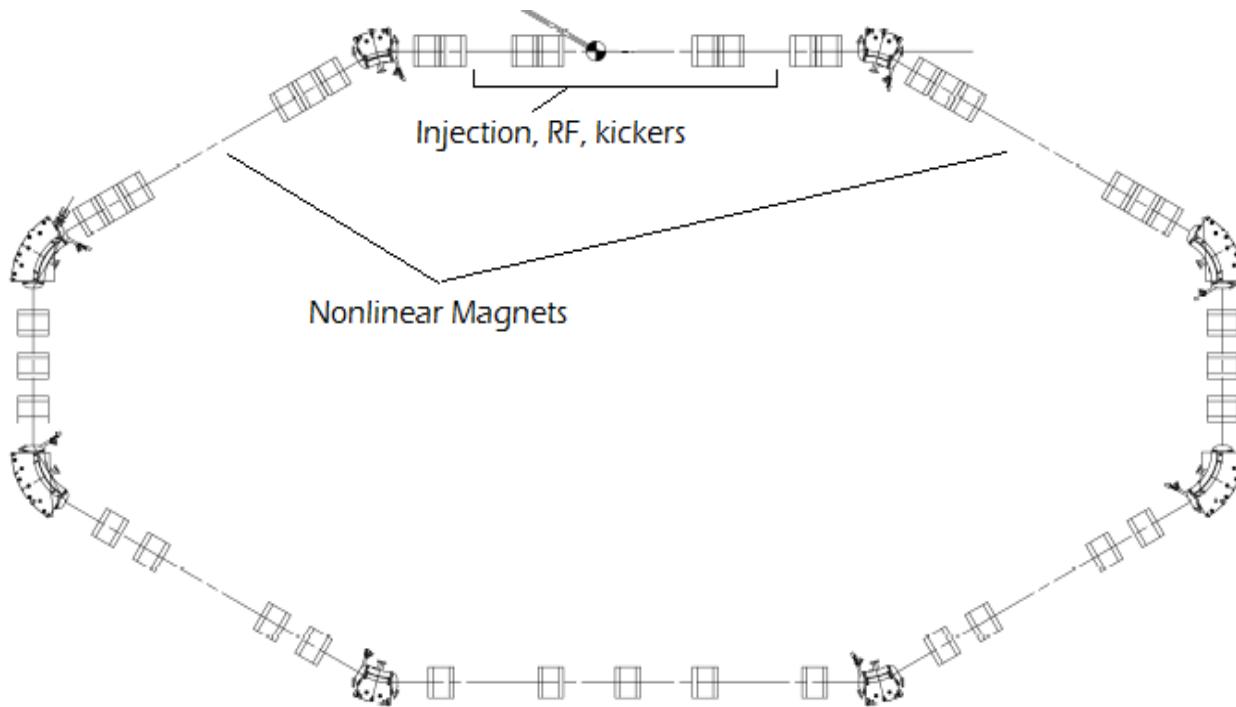
Nonlinear potential, in elliptic coordinates

- Two invariants of motion:

- 1) Hamiltonian
- 2)  $I_2(x, p_x, y, p_y)$

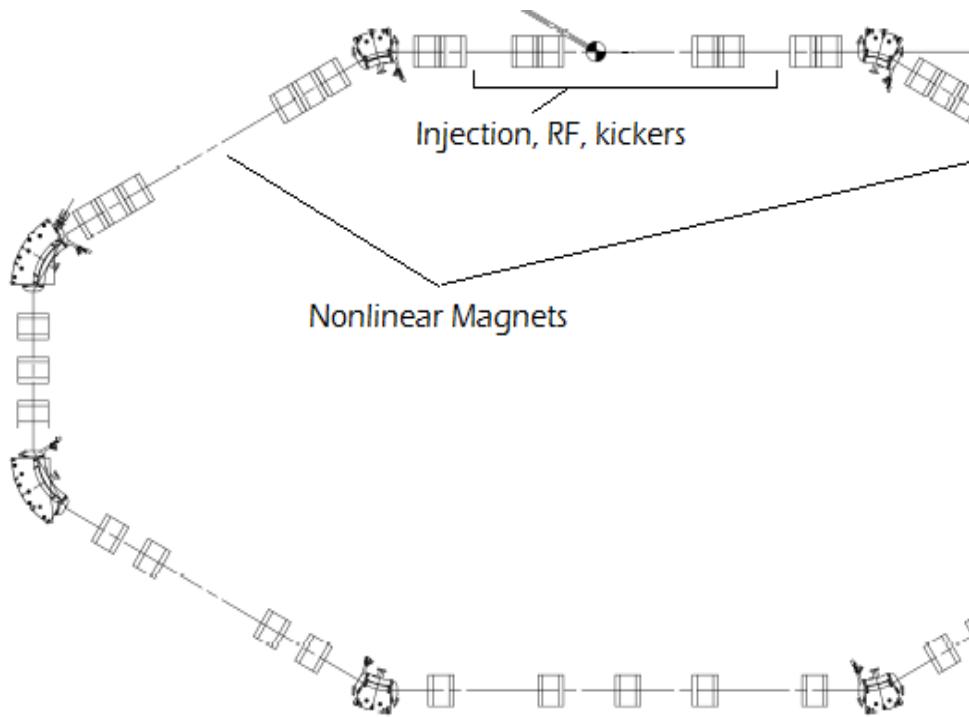
$$U(x, y) = \frac{f(\xi) - g(\eta)}{\xi^2 - \eta^2}$$

# Integrable Optics Test Accelerator



- 40 m circumference
- 4 30° and 60° dipoles
- 39 quadrupoles
- 2 drifts for nonlinear magnets

# IOTA parameters

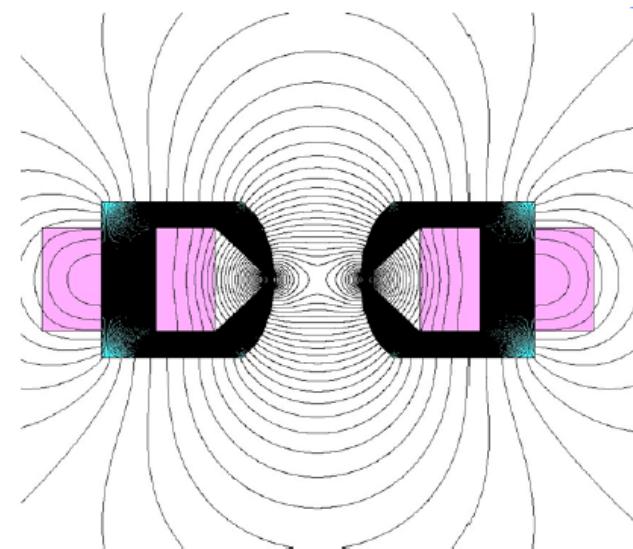


Electron Energy	150 MeV
Number of particles	$10^9$
Ring Circumference	40 m
Length of NL magnets	1.8 m
Phase advance per NL section	0.3
Synchrotron damping time	$\sim 1$ sec
Equilibrium beam size	$\sim 0.1$ mm
RF harmonic number	4
Bunch length	5 cm

# Need a special magnet

- Can we do anything with just conventional magnets?
  - Quadrupoles
  - Octupoles

Cross-section and field lines



$$U(x, y) = t \cdot \operatorname{Re} \left[ (x + iy)^2 + \frac{2}{3c^2} (x + iy)^4 + \frac{8}{15c^4} (x + iy)^6 + \frac{16}{35c^6} (x + iy)^8 + \dots \right]$$



# Quasi-integrable Optics

- Octupole magnet strength  $\sim 1/\beta(s)^3$

$$U(x_N, y_N; s) = \beta(s)V(x_N\sqrt{\beta_x(s)}, y_N\sqrt{\beta_y(s)}; s)$$
$$U = U(x_N, y_N)$$

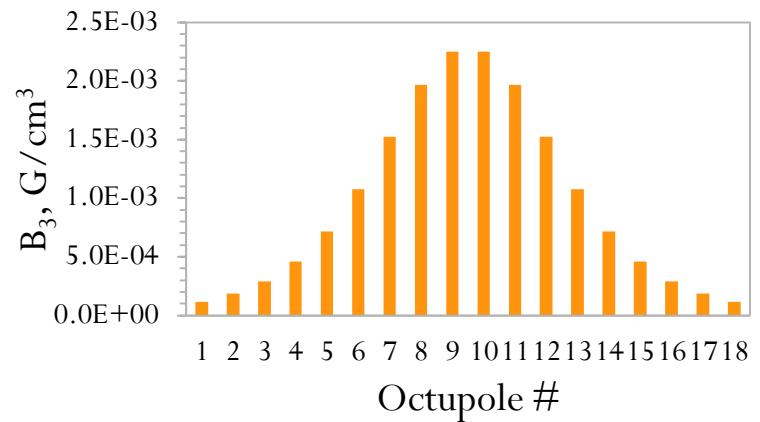
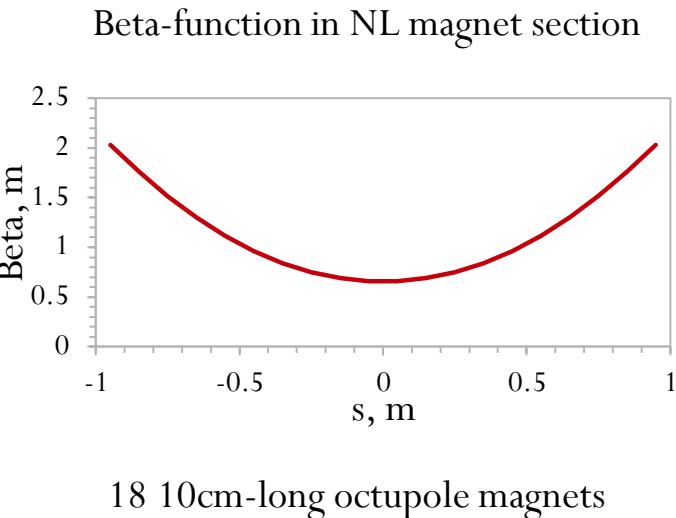
- Hamiltonian does not depend on  $s$ :

$$H = \frac{1}{2}(p_x^2 + p_y^2 + x_N^2 + y_N^2) + U(x_N, y_N)$$

- Questions:

- What about the 3<sup>rd</sup> degree of freedom?
- Imperfections

- 6D Simulations required

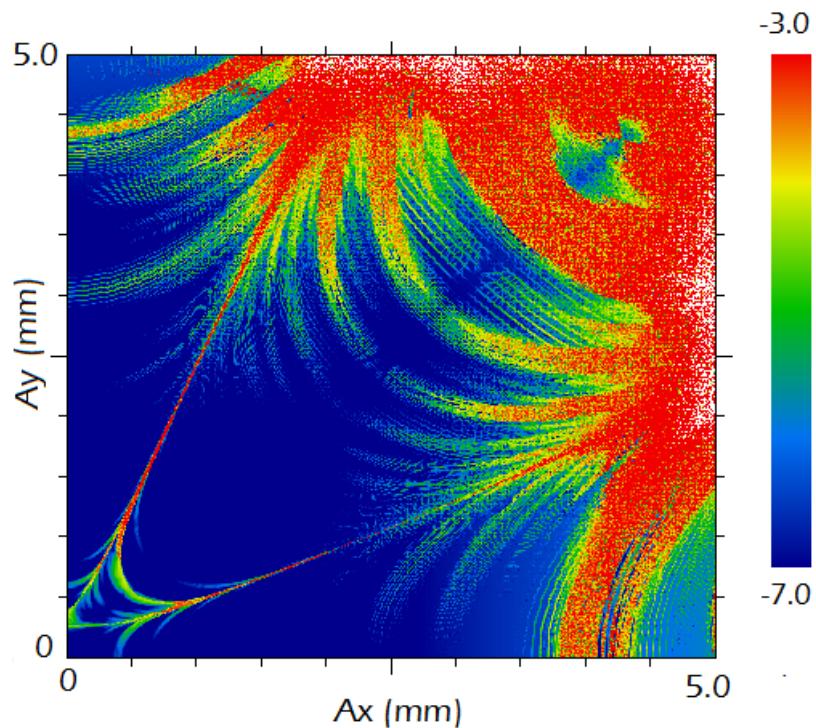


$$t = 0.4, c^2 = 0.01 \text{ cm}, l = 10 \text{ cm}$$

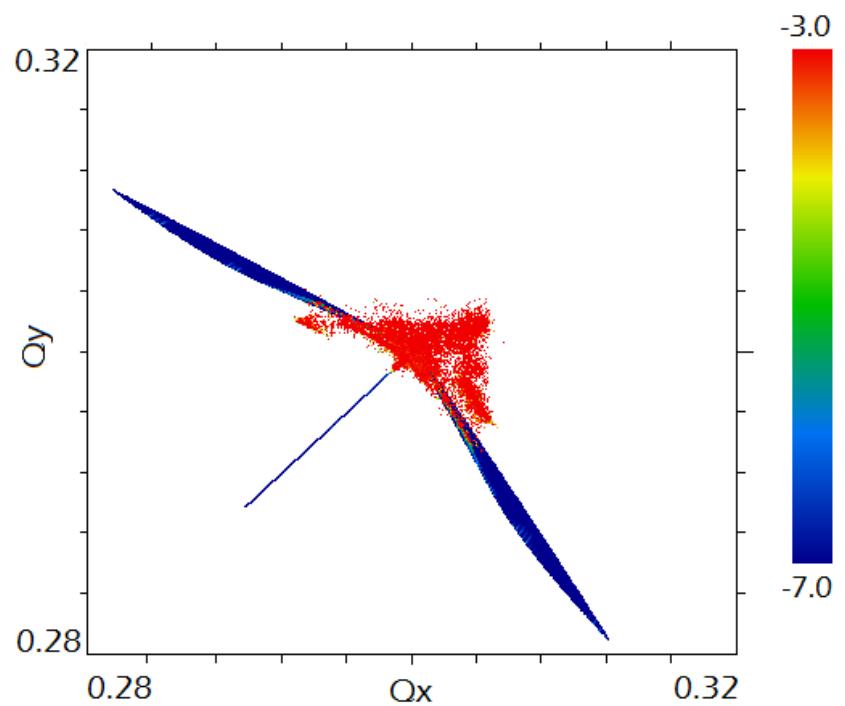
# 6D simulations

- Lifetrac code by D. Shatilov
  - Tracking
  - Frequency map analysis
- Model includes:
  - Dipoles, dipole fringe fields
  - Quadrupoles
  - RF
  - Octupoles
    - No sextupoles
- Betatron and synchrotron motion
- Chromaticity

# Frequency map analysis: 1 section, octupole magnet



Stable region:  $2.5 \times 2.5$  mm

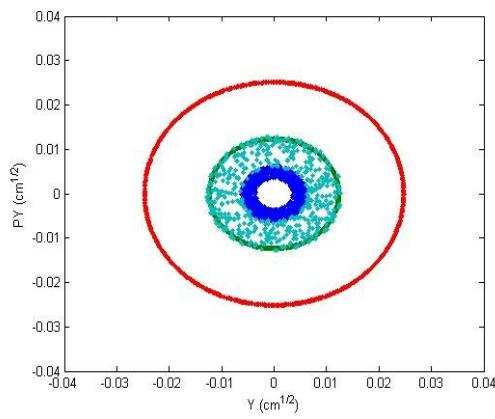
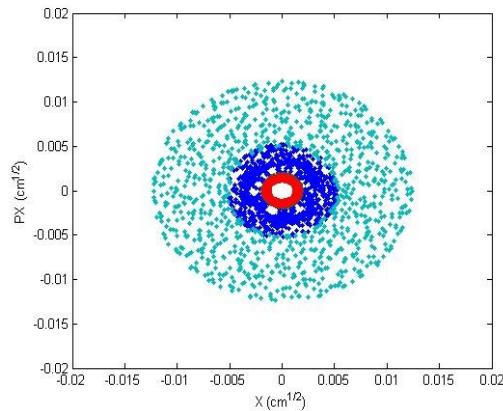


Tune spread: 0.03

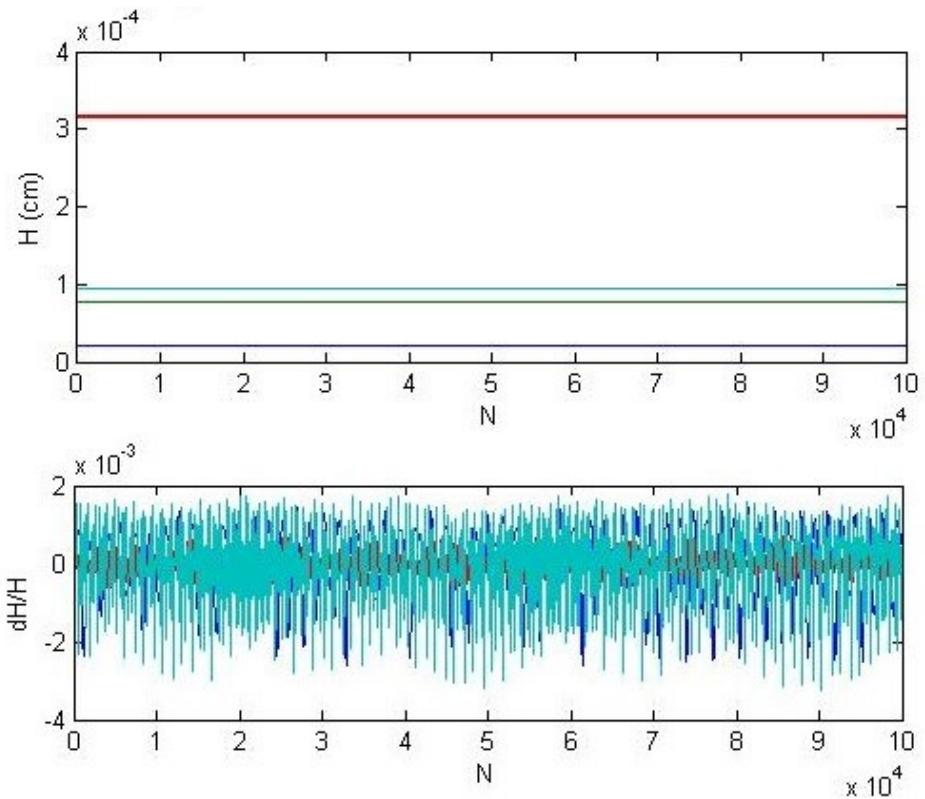
# Tracking

Simulated time – 1sec: no particles lost within stable region

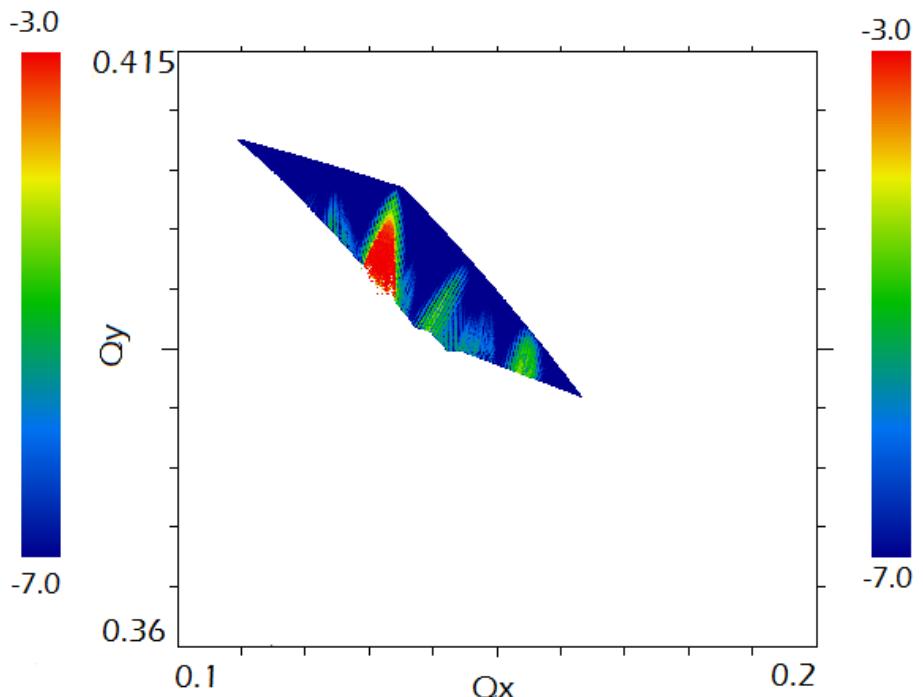
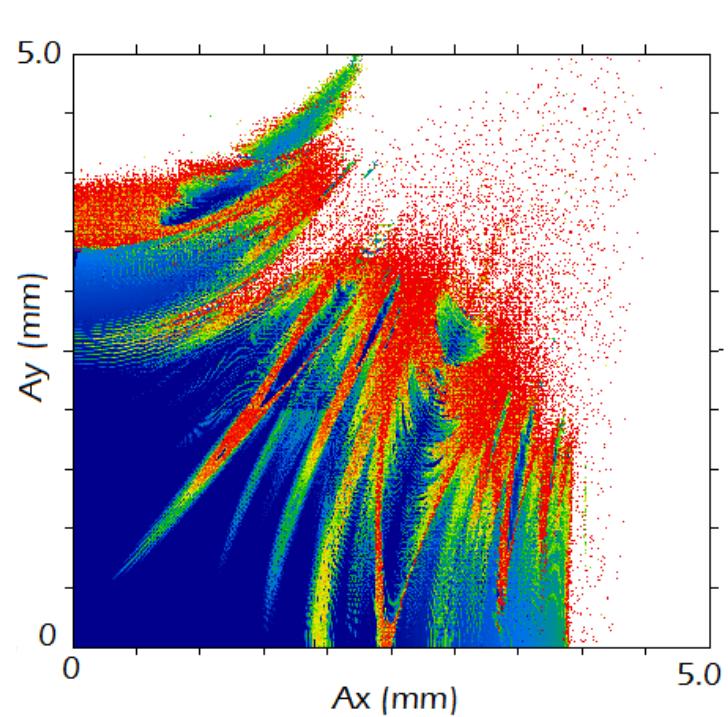
Motion is bounded



Hamiltonian is conserved



# FMA: 1 section, quadrupole + octupole

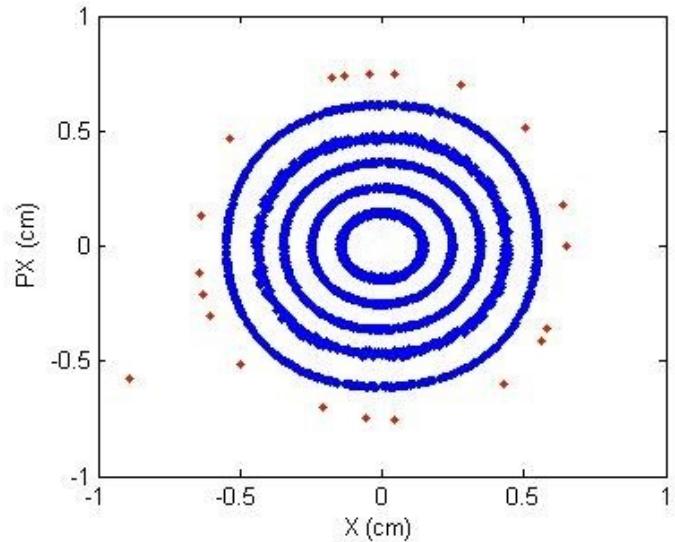


Stable region:  $2.5 \times 1.8$  mm

Tune spread: 0.05

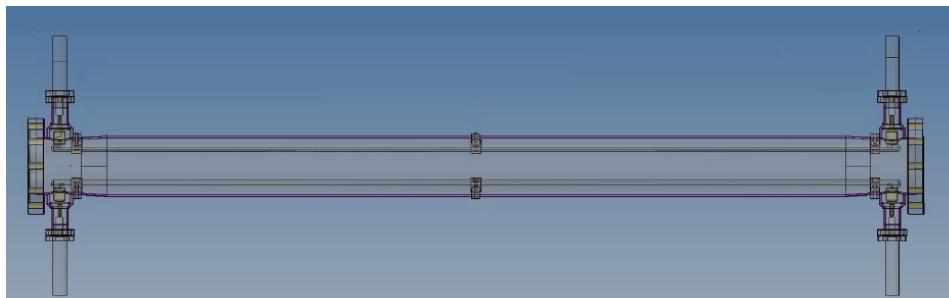
# Experimental procedure

- Two kickers, horizontal and vertical, place particles at arbitrary points in phase space
- Measure beam position on every turn to create Poincare map  $(x, y)_n$
- As electrons lose energy due to synchrotron radiation, they will cover all available phase space
- Can control the strength on the nonlinearity
- Final goal – dependence of betatron frequency on amplitude



# Two kickers create an arbitrary transverse kick

- Horizontal + vertical stripline kickers
- Rectangular pulses up to 25 kV  
~ 100 ns duration.
- Repetition rate < 1 Hz
- Adjustable voltage  $0 - V_{\max}$



Courtesy A. Didenko

Voltage  $\pm 25 \text{ kV}$

Radius:

- Pipe  $33 \text{ mm}$
- Plates  $20 \text{ mm}$

Thickness:

- Pipe  $2 \text{ mm}$
- Plates  $2 \text{ mm}$

Opening angle  $70 \text{ deg}$

Edge rounding radius  $3 \text{ mm}$

Wave impedance:

- Odd mode  $50 \text{ Ohm}$
- Even mode  $55 \text{ Ohm}$

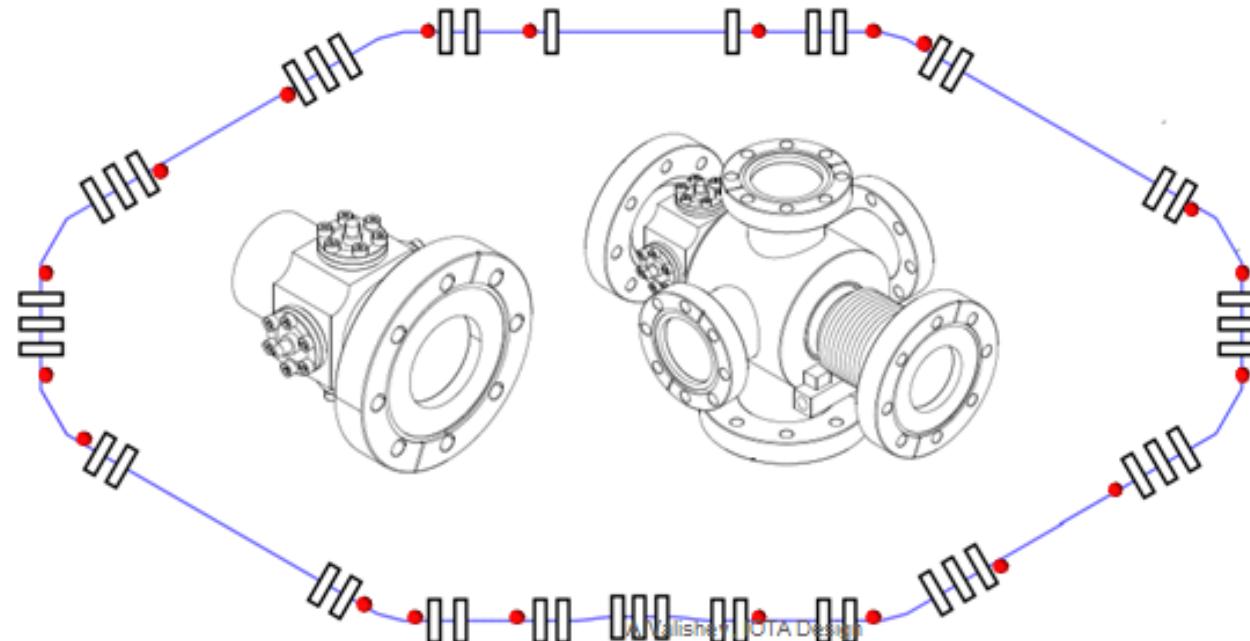
E-field in the center  $12 \text{ kV/cm}$

Length:

- Horizontal  $55 \text{ cm}$
- Vertical  $100 \text{ cm}$

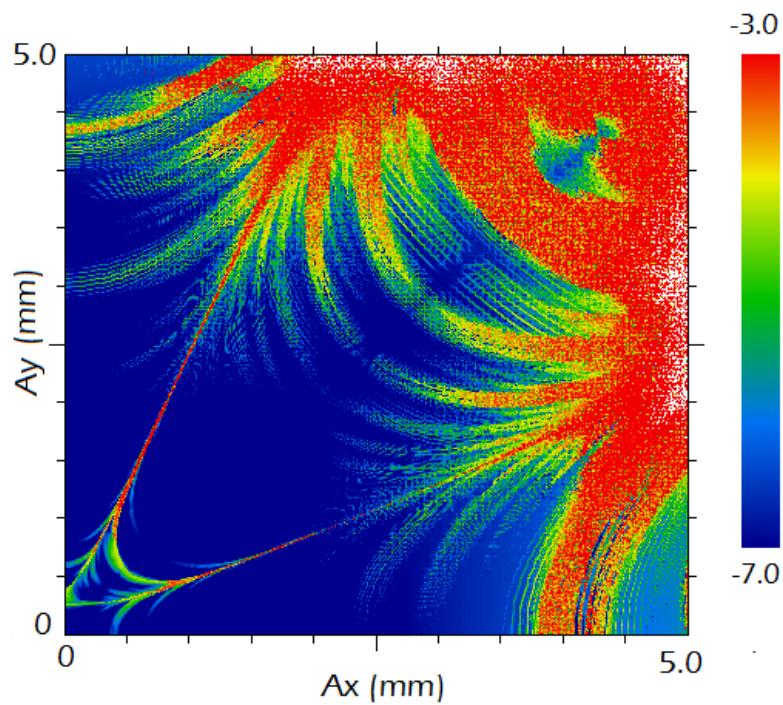
# Beam position can be measured precisely

- 20 horizontal and vertical BPMs
  - Button type
  - $1 \mu\text{m}$  closed orbit resolution
  - $100 \mu\text{m}$  turn-by turn resolution
- 8 SR ports to measure beam size

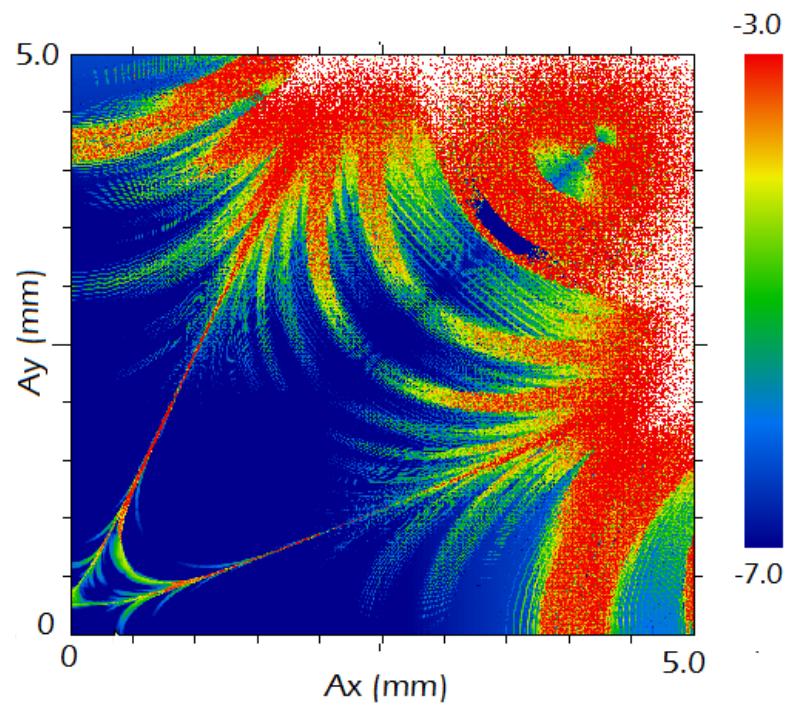


# Octupole imperfections: stable region reduces insignificantly

No imperfections

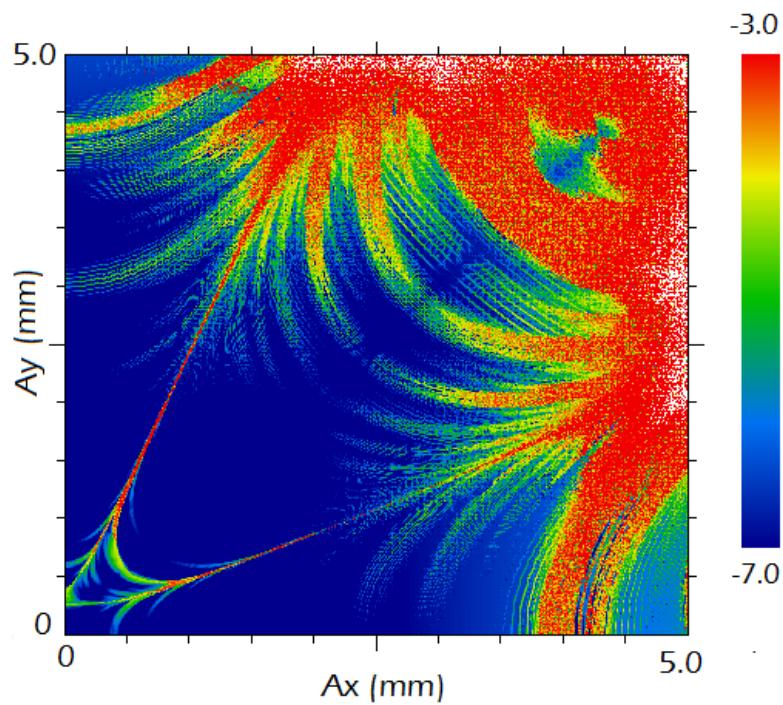


Octupole error,  $\sigma = 0.1$

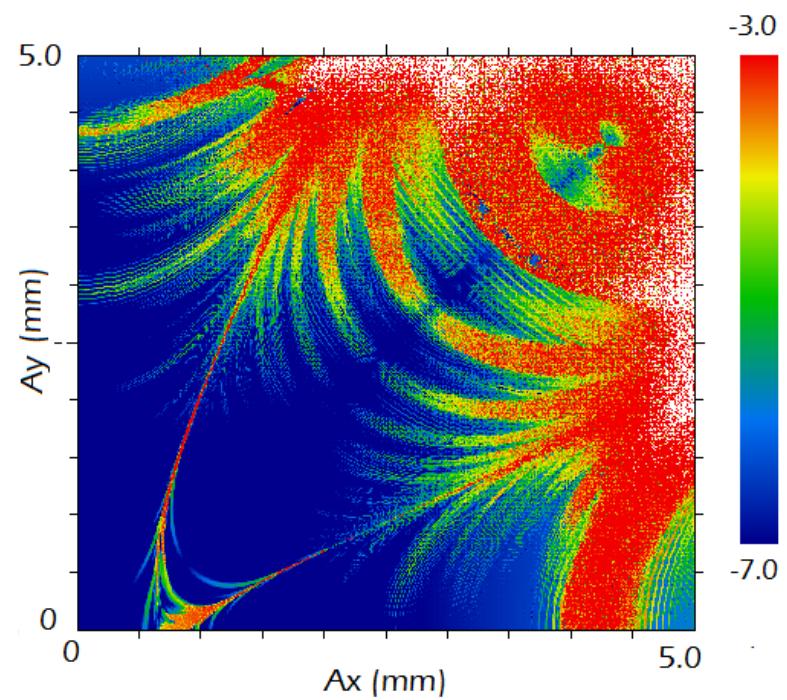


# Lattice imperfections: stable region reduces insignificantly

No imperfections



$\Delta\beta = 1\%, \Delta\Phi = 3 \cdot 10^{-3}$



# Sources of error

- Lattice imperfections
  - Beta functions: 0.01 (relative)
  - Phase advance: 0.001
- Octupole magnet errors
  - Less than 0.1
- Bunch transverse size
  - $\sim 0.1$  mm, RMS
- Other:
  - BPM resolution
  - FFT
  - Energy loss

Overall:  $\delta A \sim 0.1$  mm,  $\delta Q \sim 10^{-3}$

# Summary

- It is possible to achieve tune spreads  $\sim 10^{-2}$  with just conventional magnet components and still retain large dynamic aperture

# Next steps

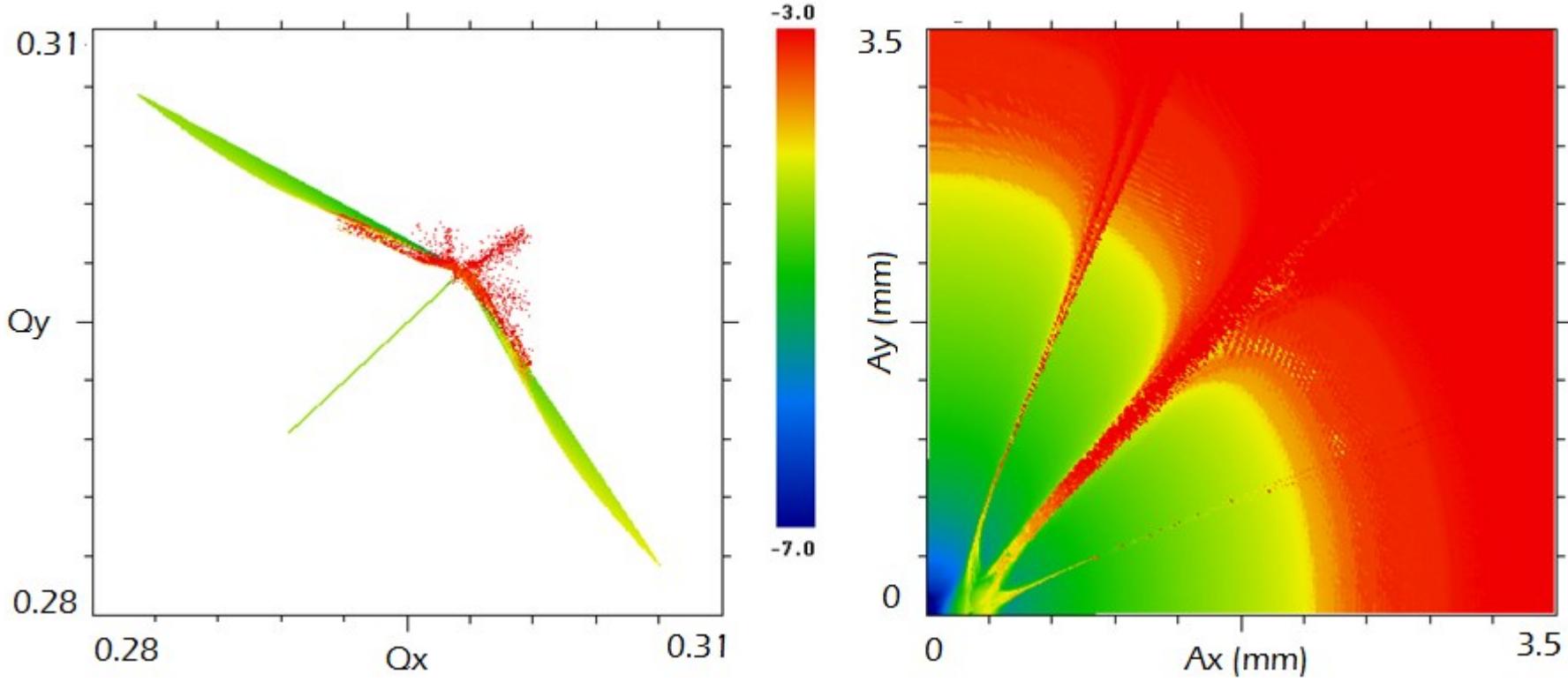
- Search for optimal combination in terms of tune spread/size of dynamic aperture/complexity of the potential
- Compare with full nonlinear potential

Thank You for Your Attention

# Backup slides

# Thick octupoles

- While dynamic aperture is limited, the attainable tune spread remains large



Courtesy A. Valishev

# Optic functions in the nonlinear section

- Equal beta functions in x and y
- Zero dispersion

